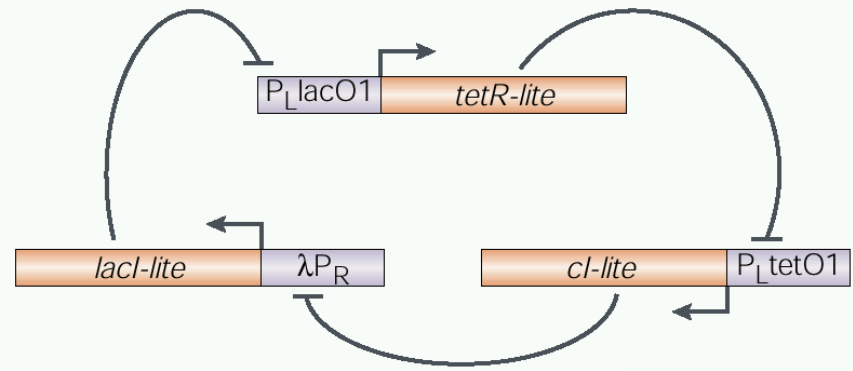
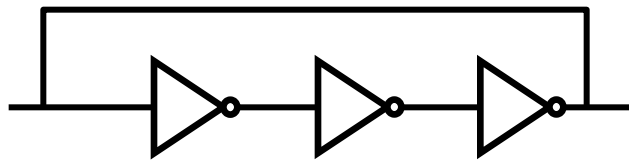


Evolution of synthetic oscillators

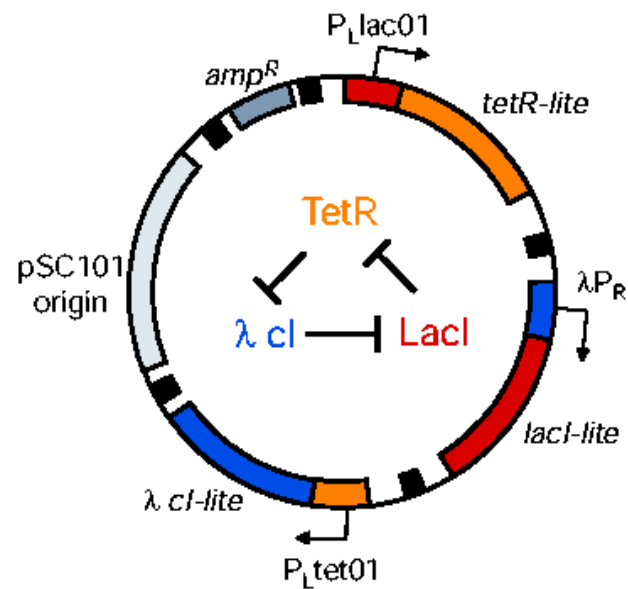
Year	Lab	Description
2000	Leibler	Repressilator
2003	Ninfa	Relaxation (activator/inhibitor)
2005	Liao	Metabollator
2009	Hasty	Tunable relaxation oscillator
2009	Fussenegger	Mammalian oscillator
2010	Hasty	Synchronized oscillator

The Ring Oscillator

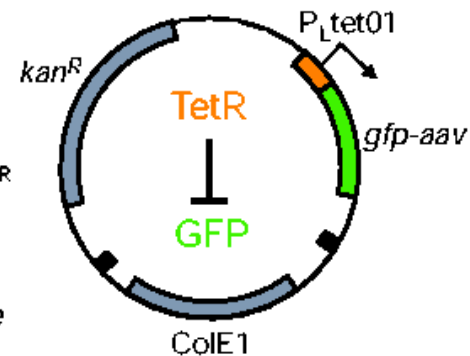
[Elowitz, Leibler 2000]



Repressilator



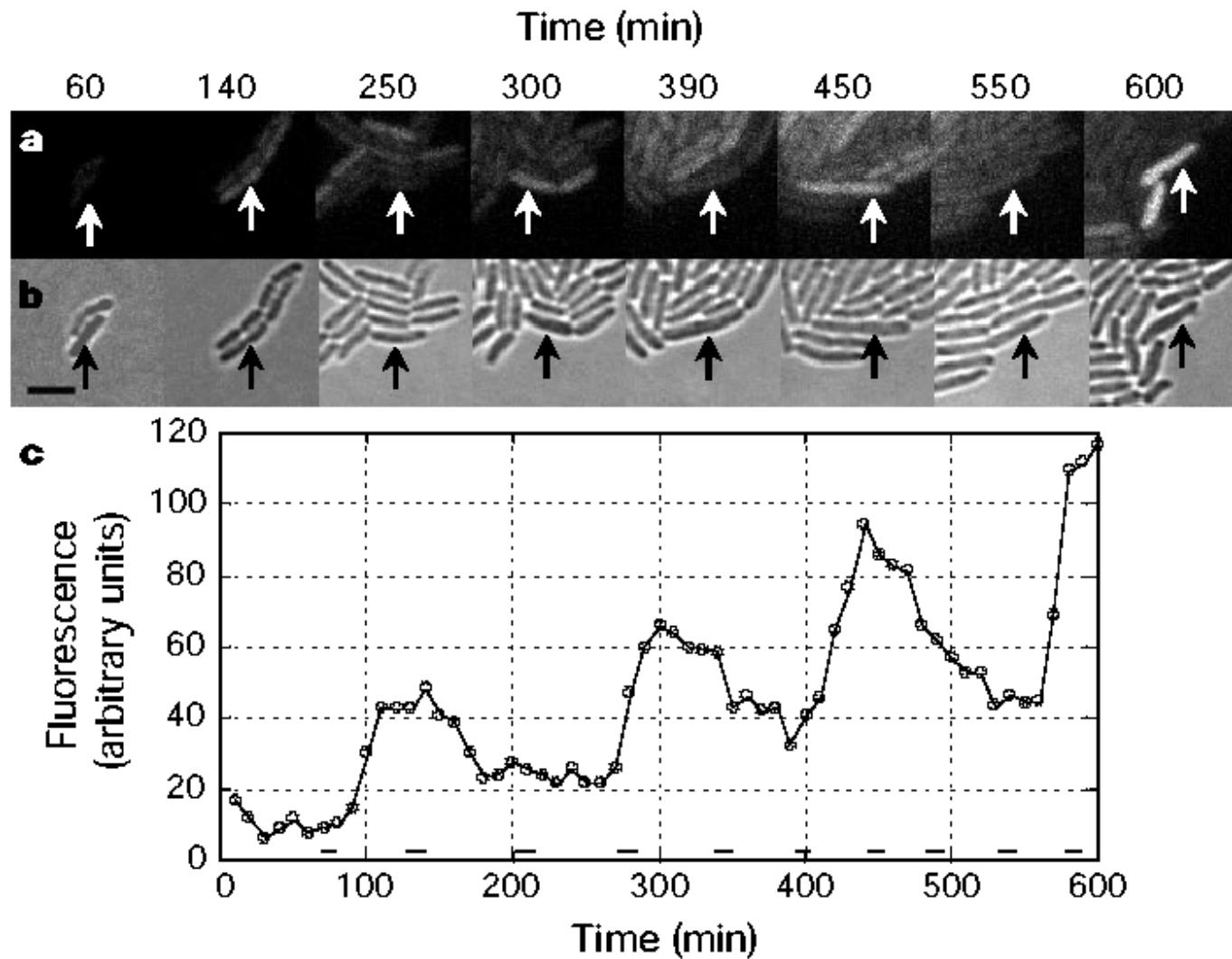
Reporter



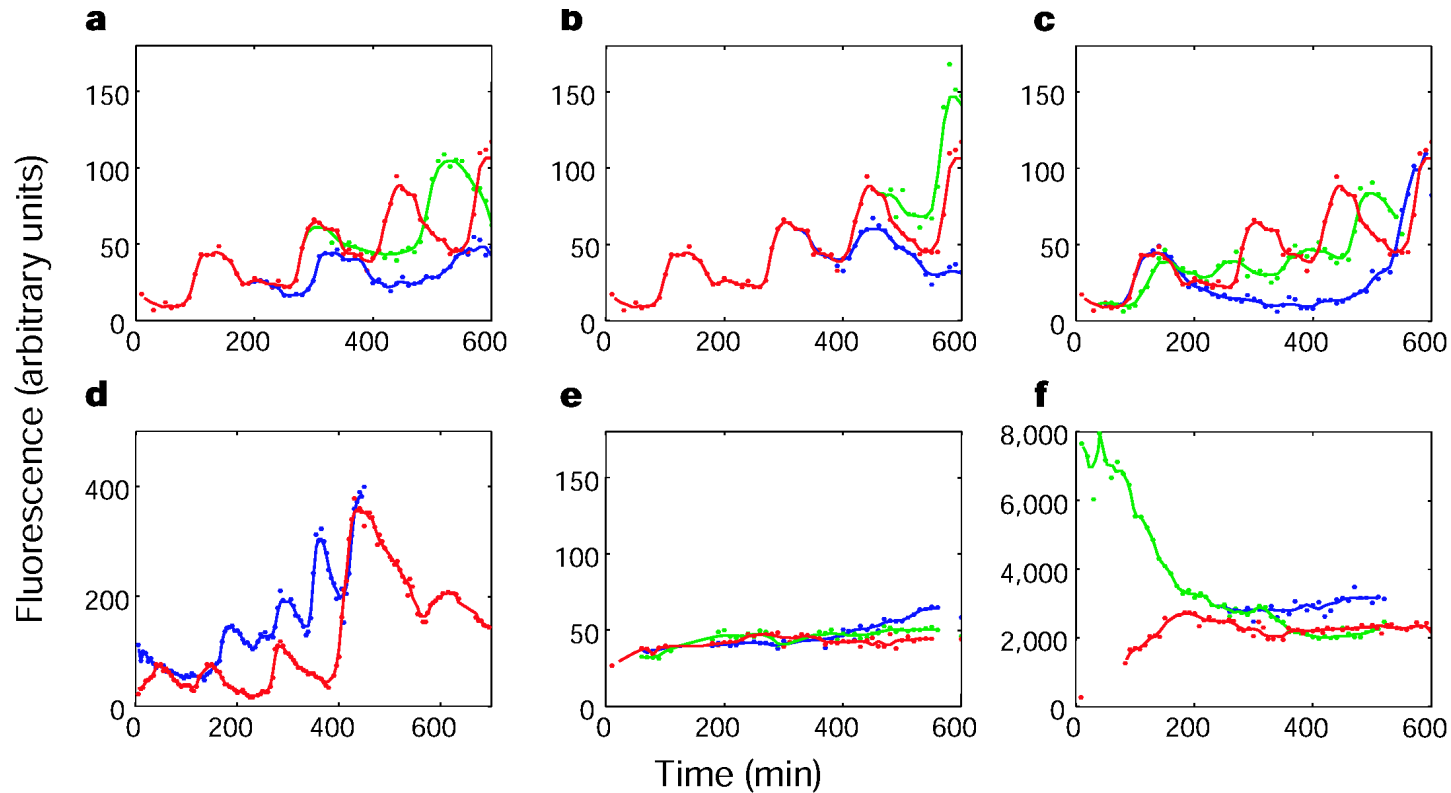


Courtesy: Michael Elowitz

Example of Oscillation



Evaluation of the Ring Oscillator

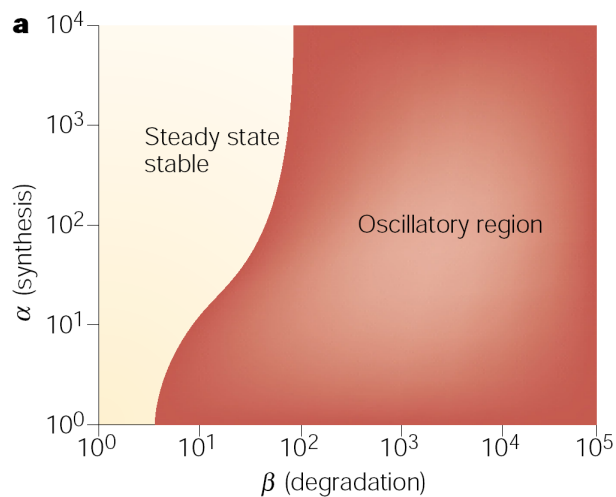


[Elowitz & Leibler, 2000]

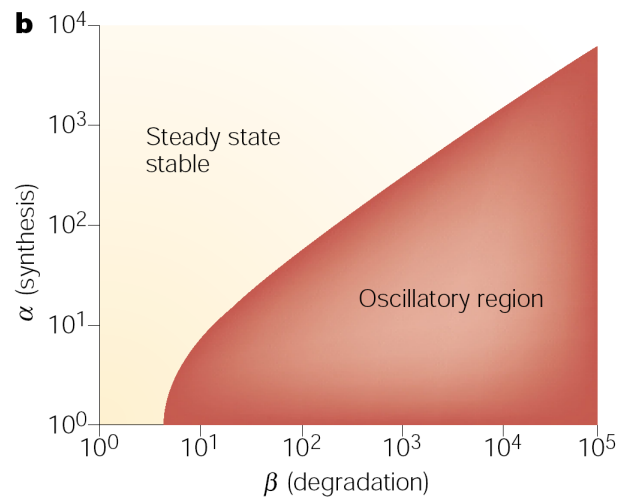
- Reliable long-term oscillation doesn't work yet
- Need to match gates, maybe use other network motifs

Requirements for Oscillation

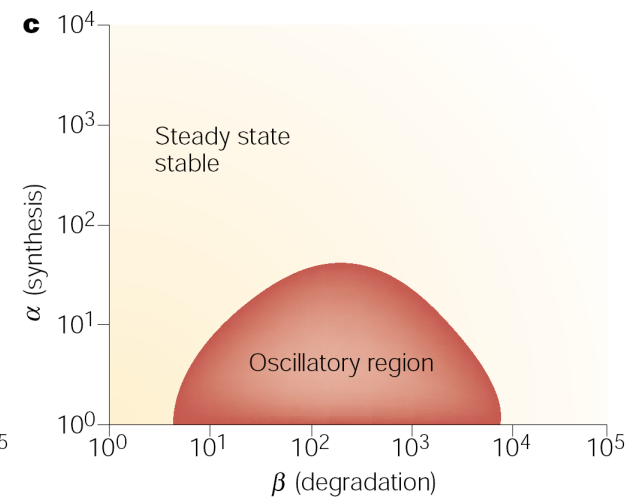
$$\begin{aligned} \frac{dm_i}{dt} &= -m_i + \frac{\alpha}{(1+p_i^n)} + \alpha_0 & \left(\begin{array}{l} i = lacI, tetR, cl \\ j = cl, lacI, tetR \end{array} \right) \\ \frac{dp_i}{dt} &= -\beta(p_i - m_i) \end{aligned}$$



$$n = 2.1, \alpha_0 = 0$$



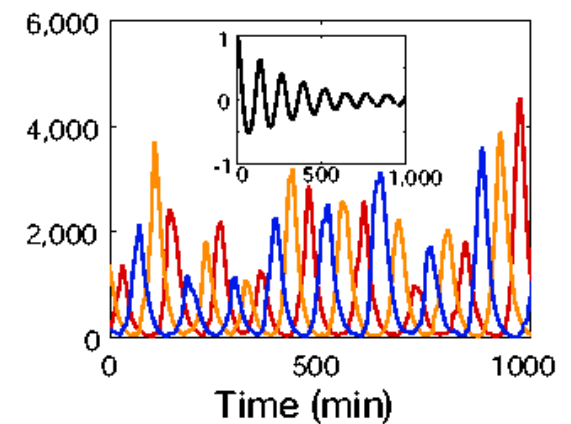
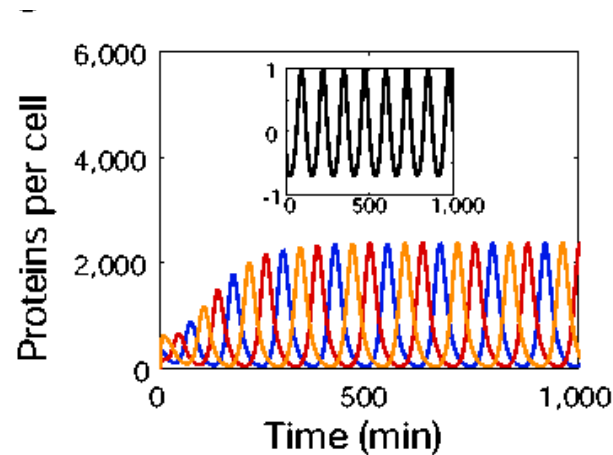
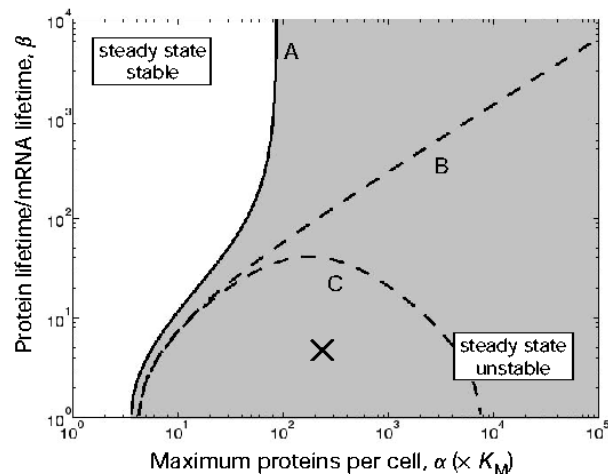
$$n = 2.0, \alpha_0 = 0$$



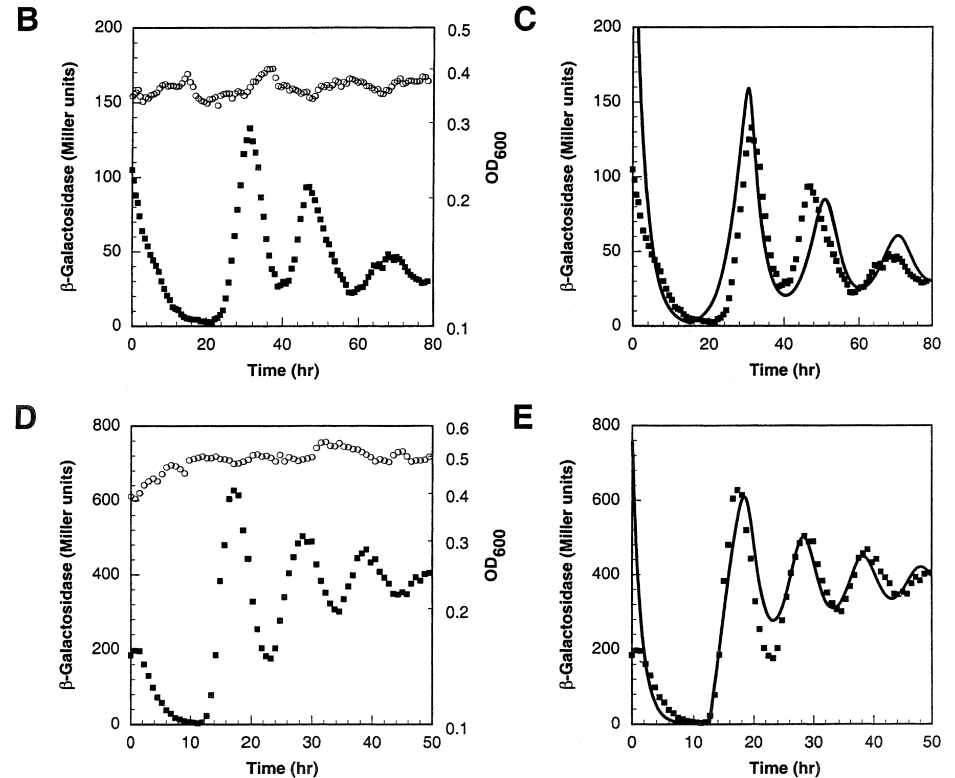
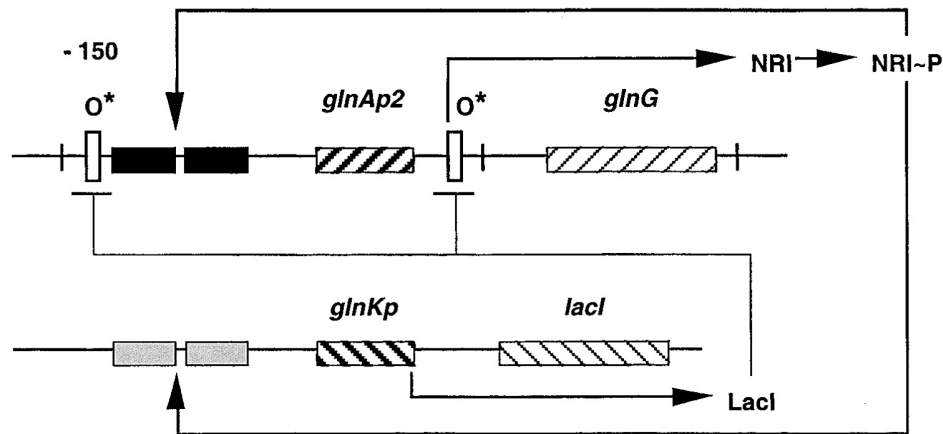
$$n = 2.0, \alpha_0/\alpha = 10^{-3}$$

Analysis of Oscillation

$$\begin{aligned} \frac{dm_i}{dt} &= -m_i + \frac{\alpha}{(1 + p_i^n)} + \alpha_0 & \left(i = lacI, tetR, cl \right) \\ \frac{dp_i}{dt} &= -\beta(p_i - m_i) & \left(j = cl, lacI, tetR \right) \end{aligned}$$

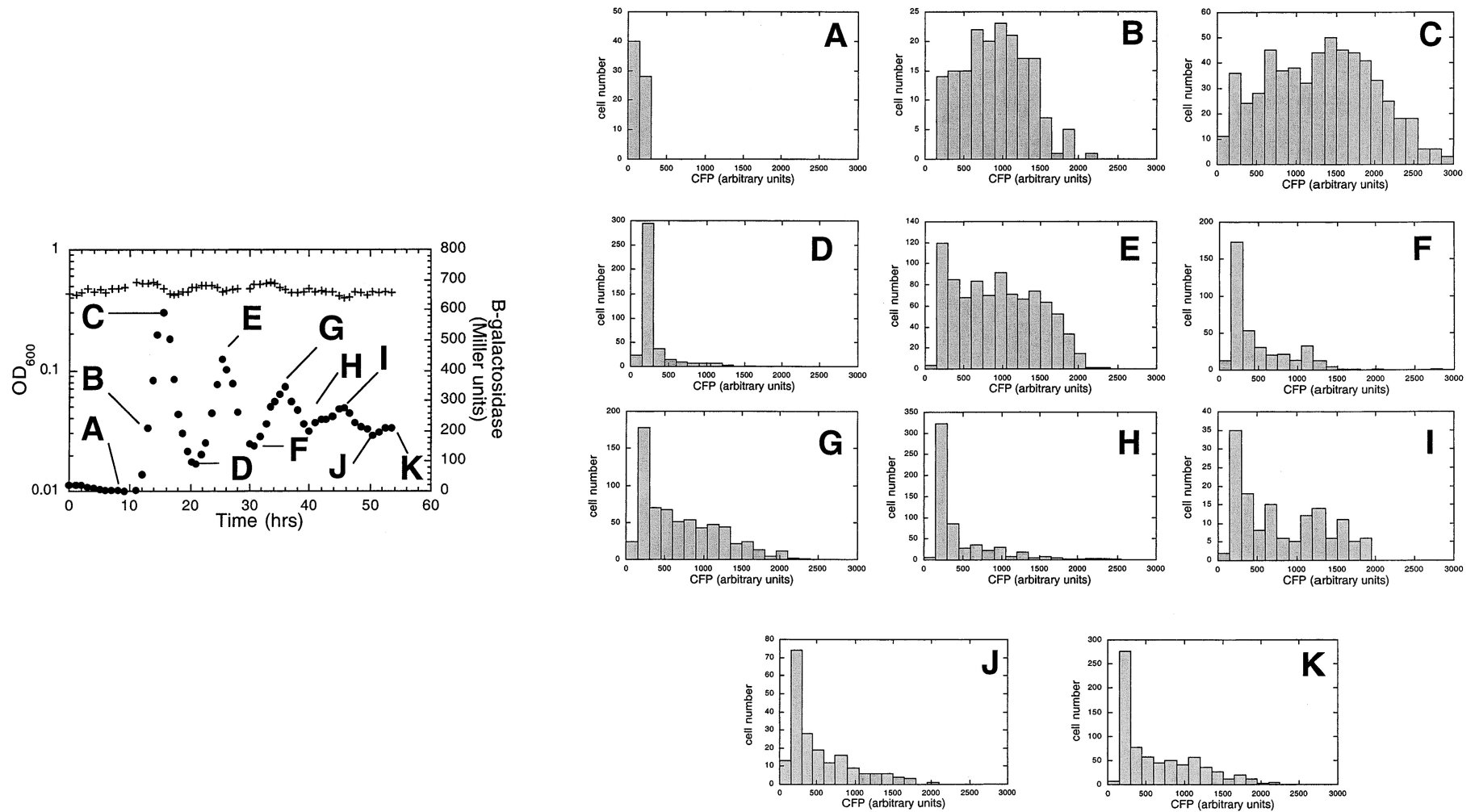


Ninfa's Genetic Clock

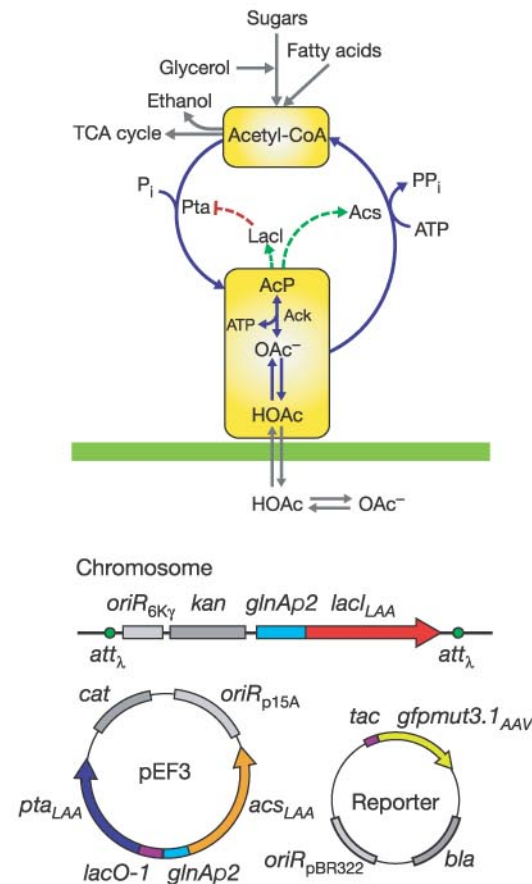
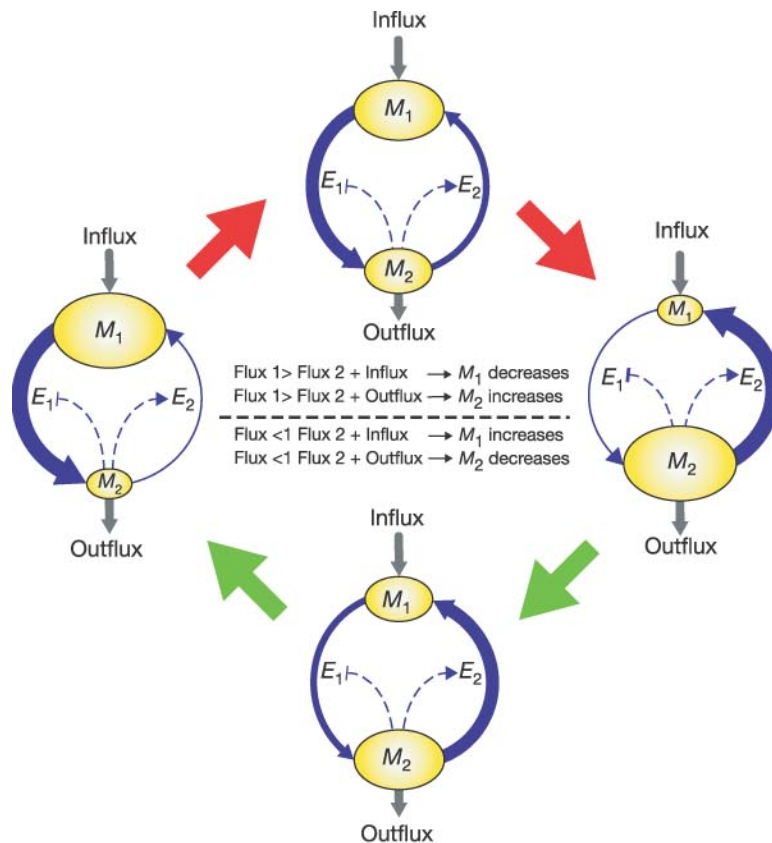


Mariette R. Atkinson, Michael A. Savageau, Jesse T. Myers,^{2,3} and Alexander J. Ninfa, Development of Genetic Circuitry Exhibiting Toggle Switch or Oscillatory Behavior in *Escherichia coli*, Cell, Vol. 113, 597–607, 2003

Single cell statistics

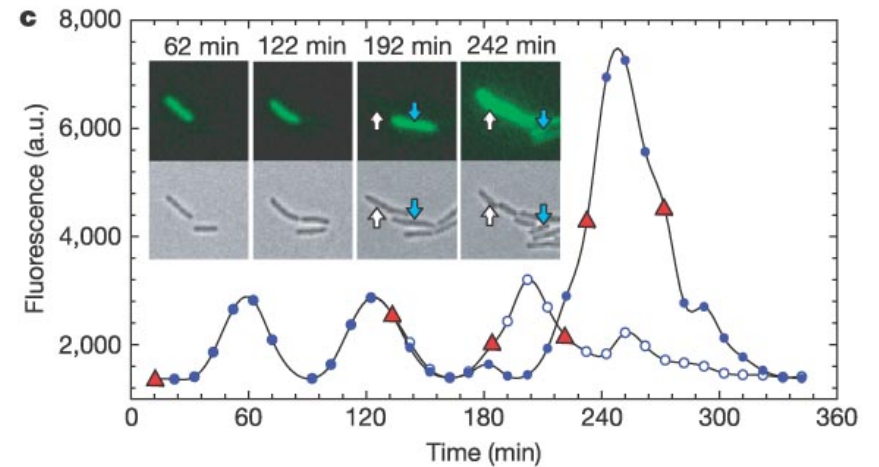
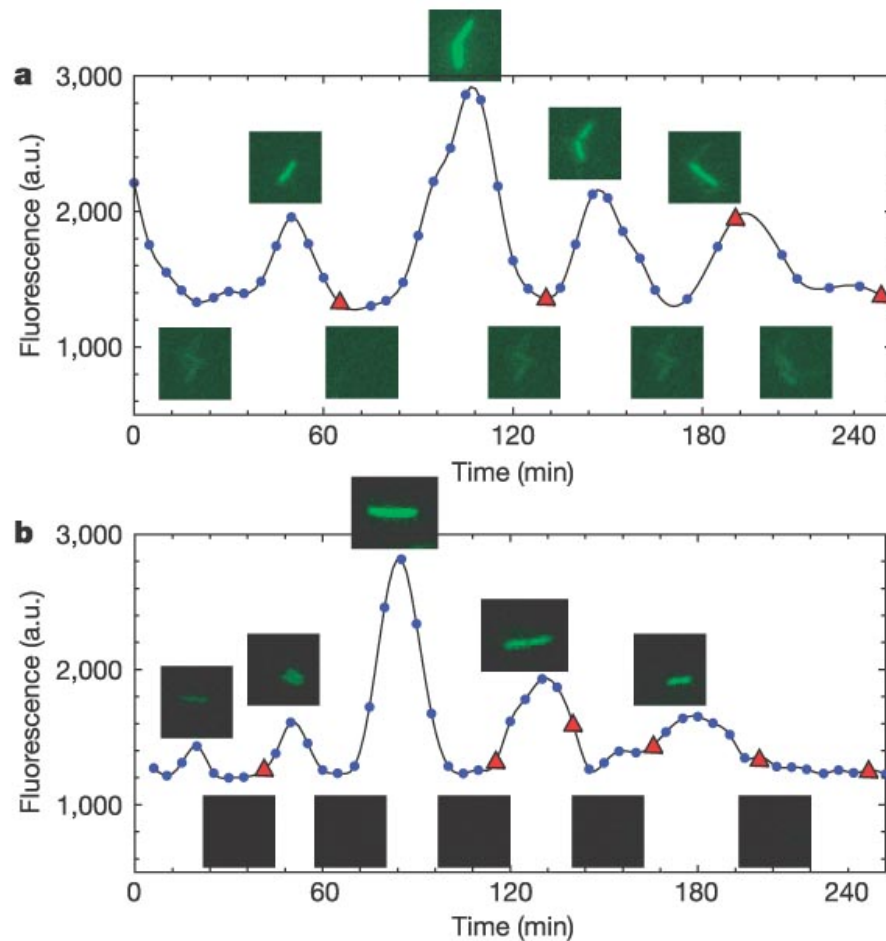


Metabolic Oscillator

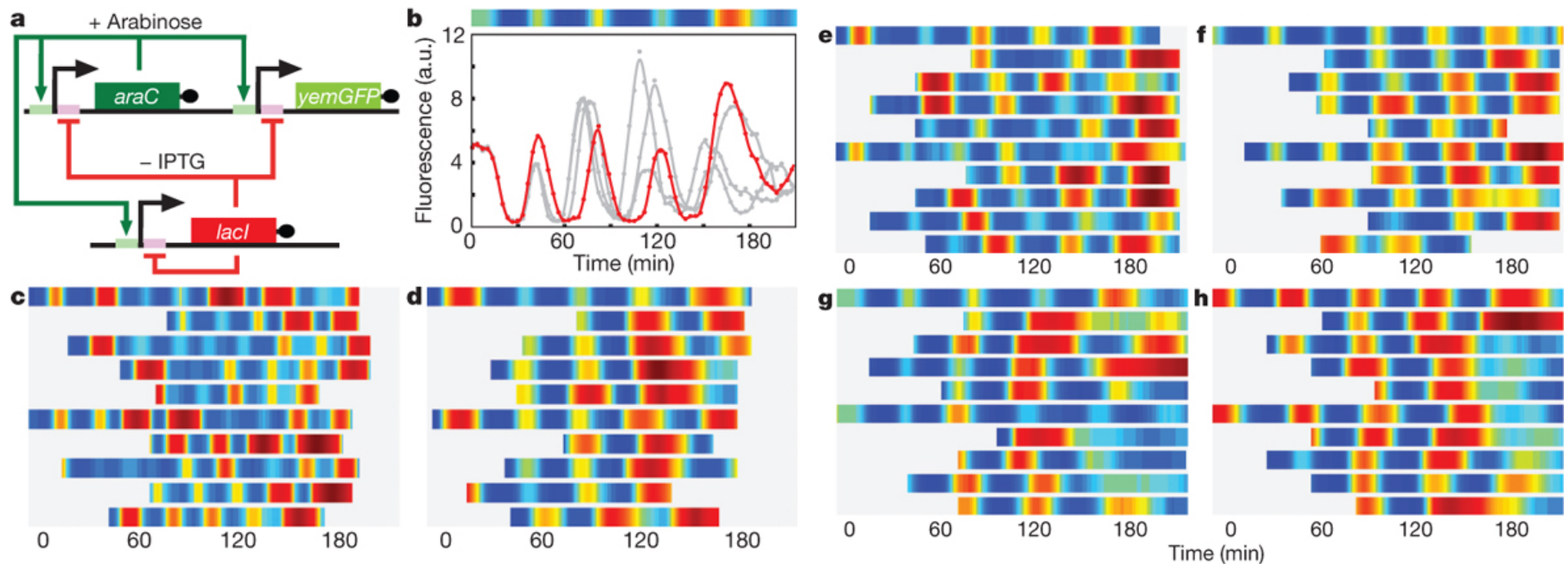


Eileen Fung, Wilson W. Wong, Jason K. Suen, Thomas Bultter, Sun-gu Lee & James C. Liao, A synthetic gene-metabolic Oscillator. Nature, VOL 435 (2005)

Metabollator Dynamics

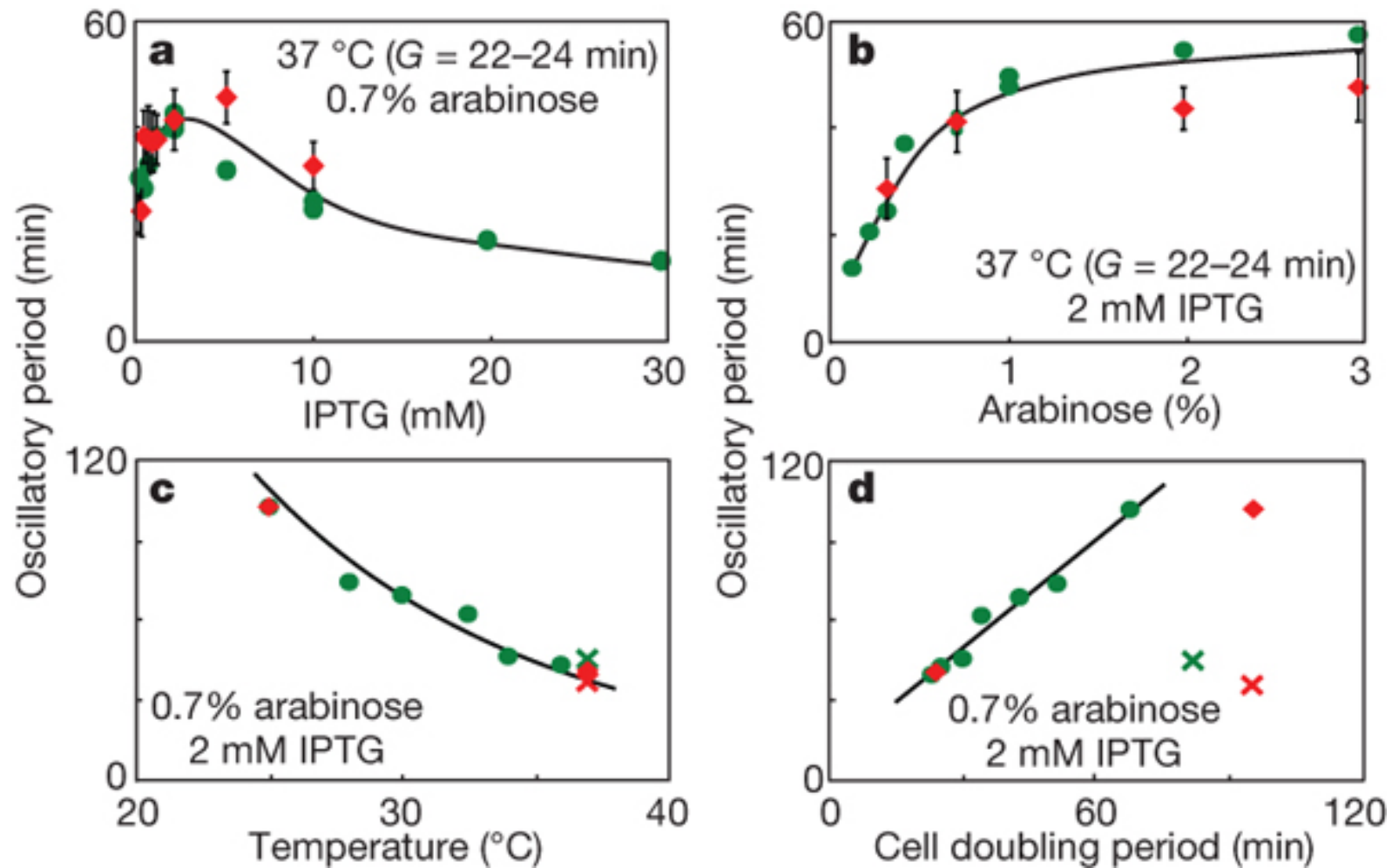


A Tunable Oscillator

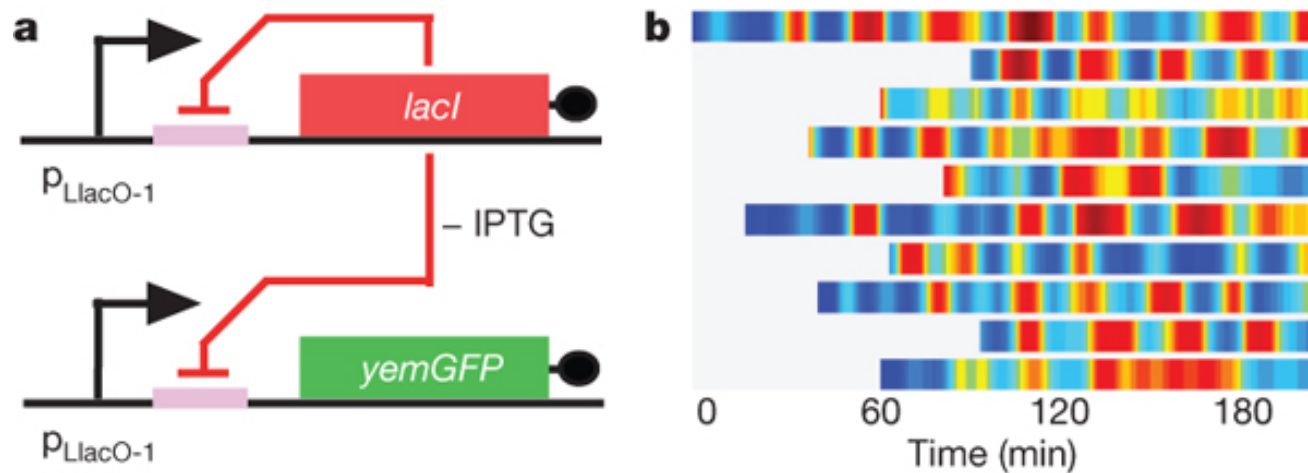


Jesse Stricker, Scott Cookson, Matthew R. Bennett, William H. Mather, Lev S. Tsimring & Jeff Hasty, A fast, robust and tunable synthetic gene oscillator Nature, Vol 456|27, 2008

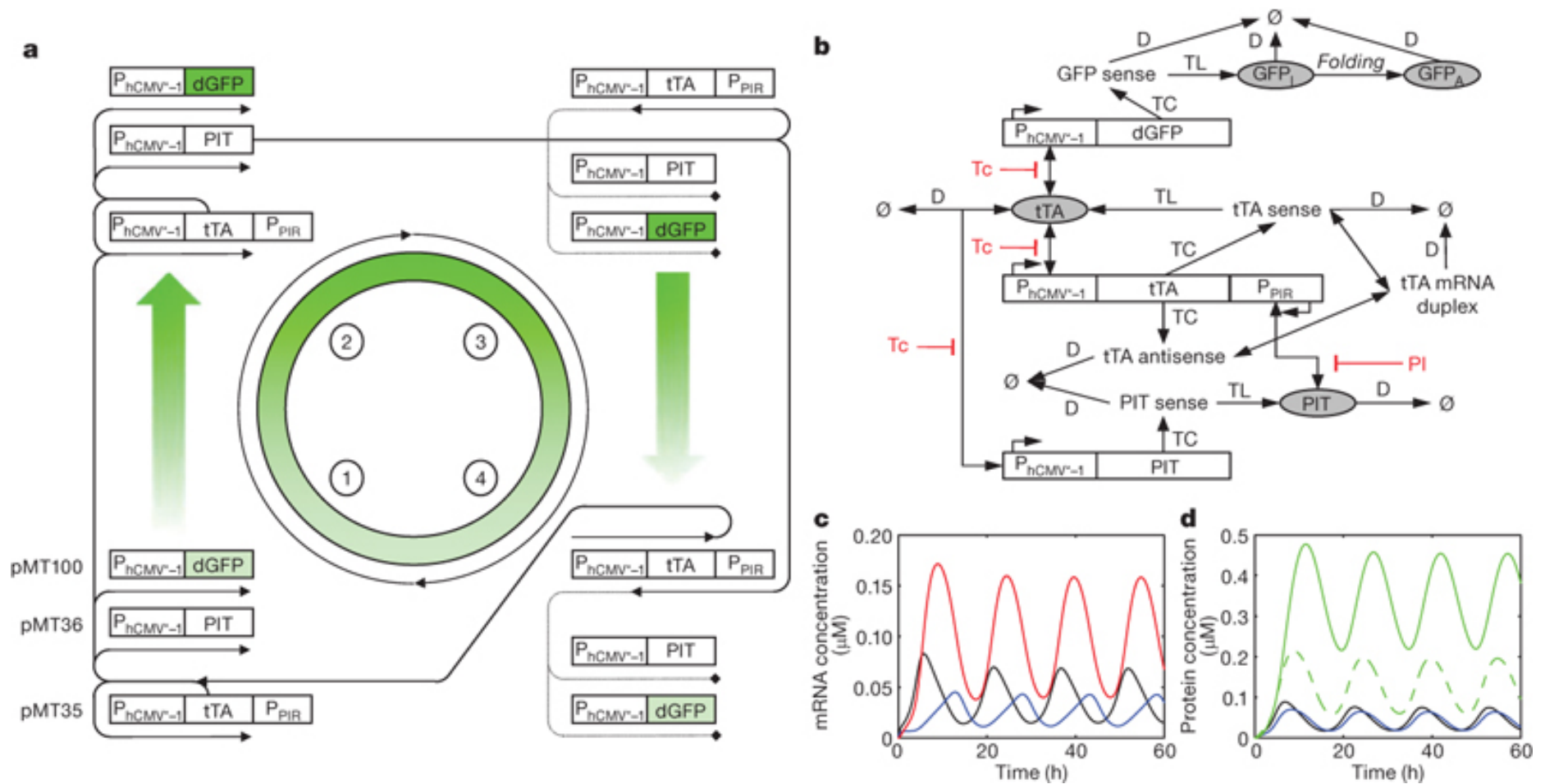
A Tunable Oscillator



An oscillator with no positive feedback loop

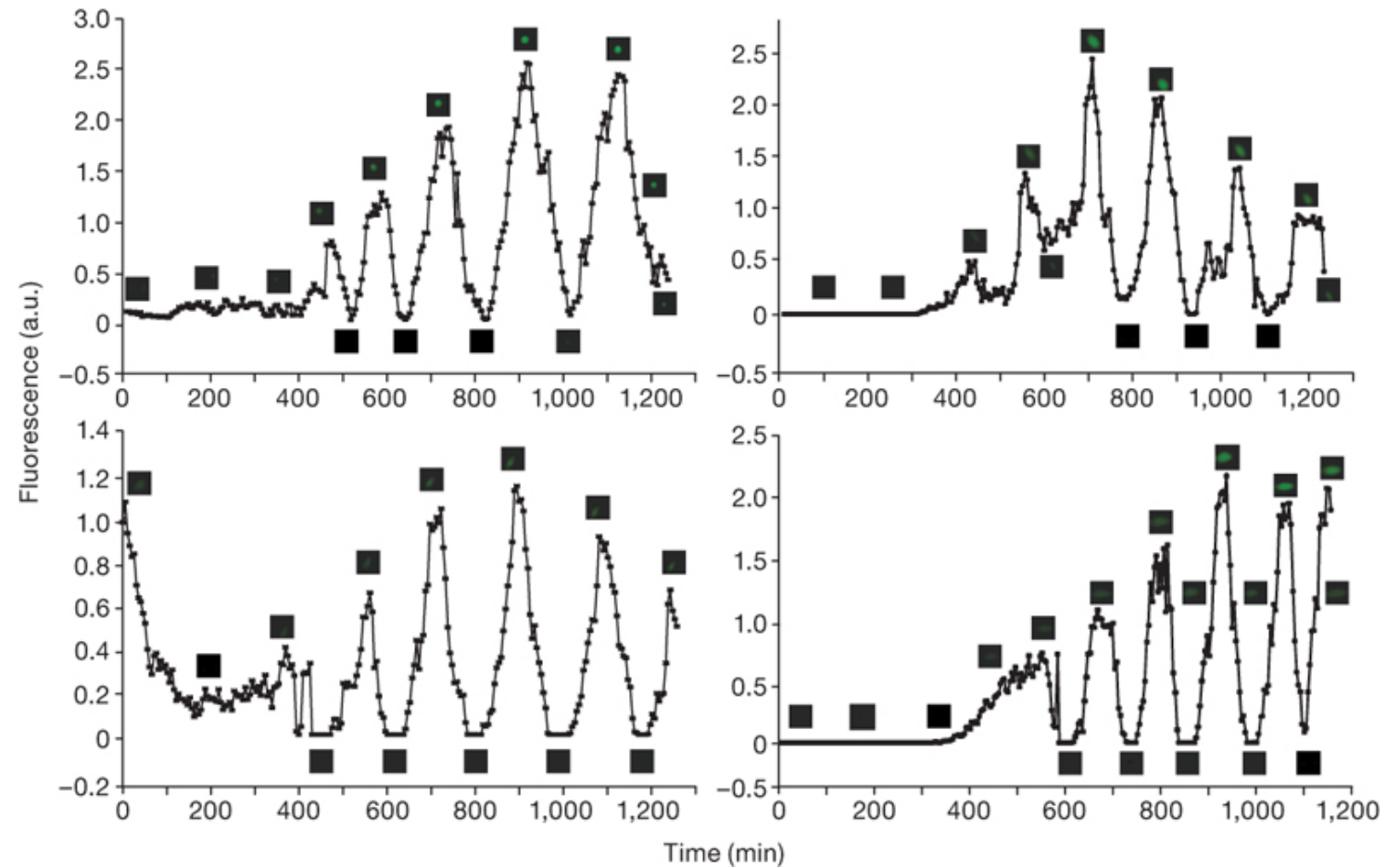


A mammalian oscillator

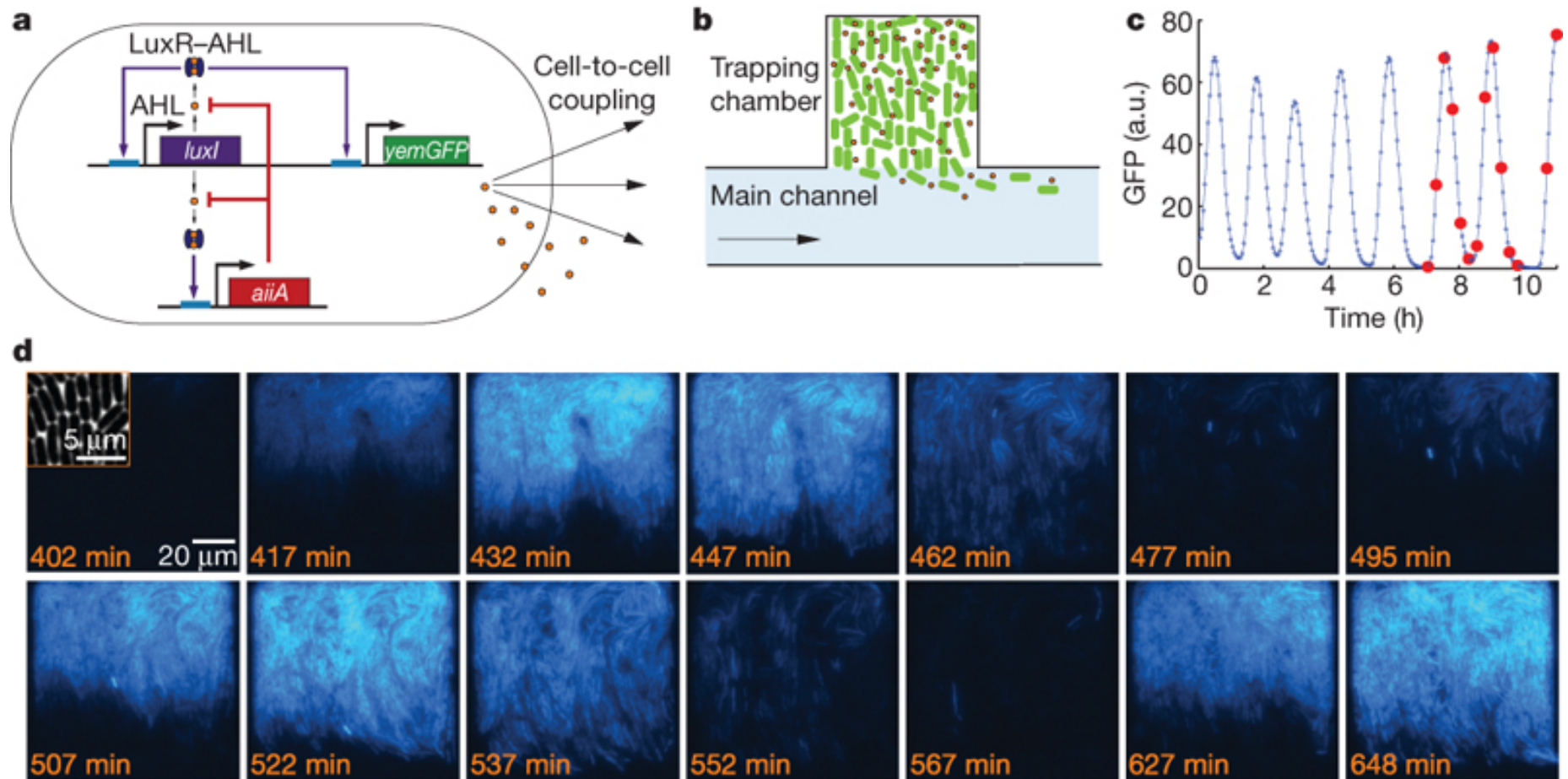


Marcel Tigges, Tatiana T. Marquez-Lago, Joerg Stelling & Martin Fussenegger, A tunable synthetic mammalian oscillator, *Nature*, Vol 457, 2009

Single cell behaviors

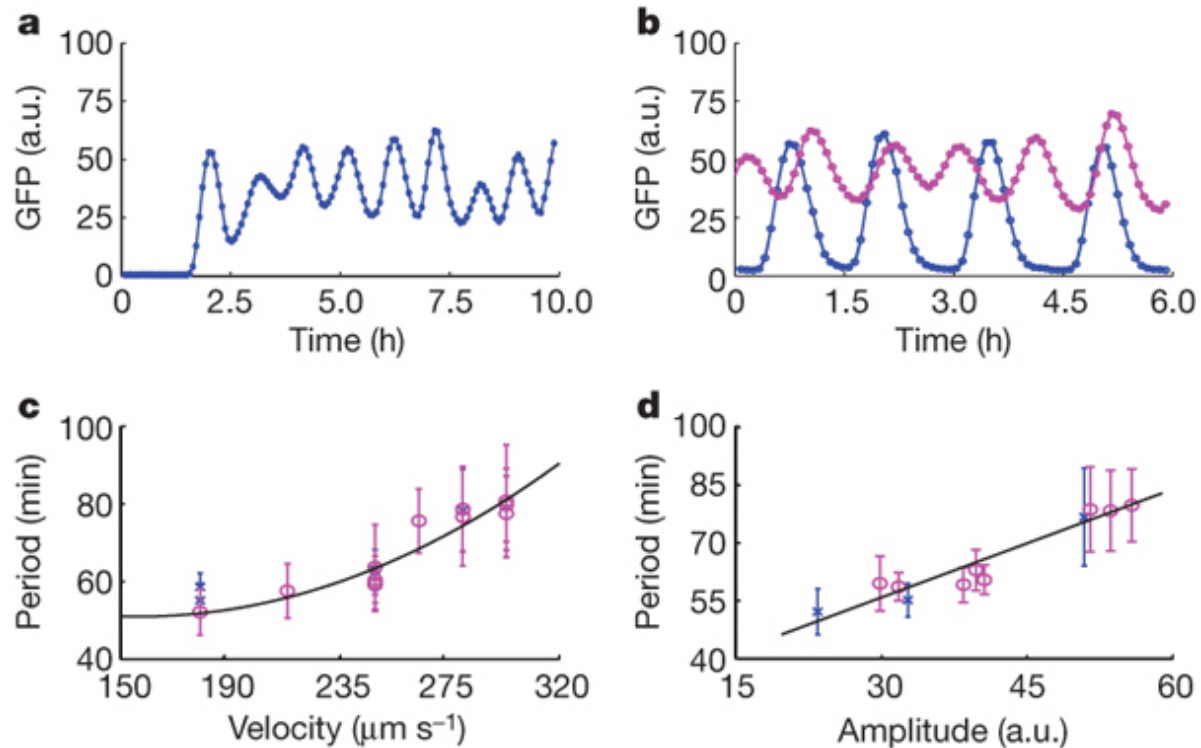


Synchronized oscillators

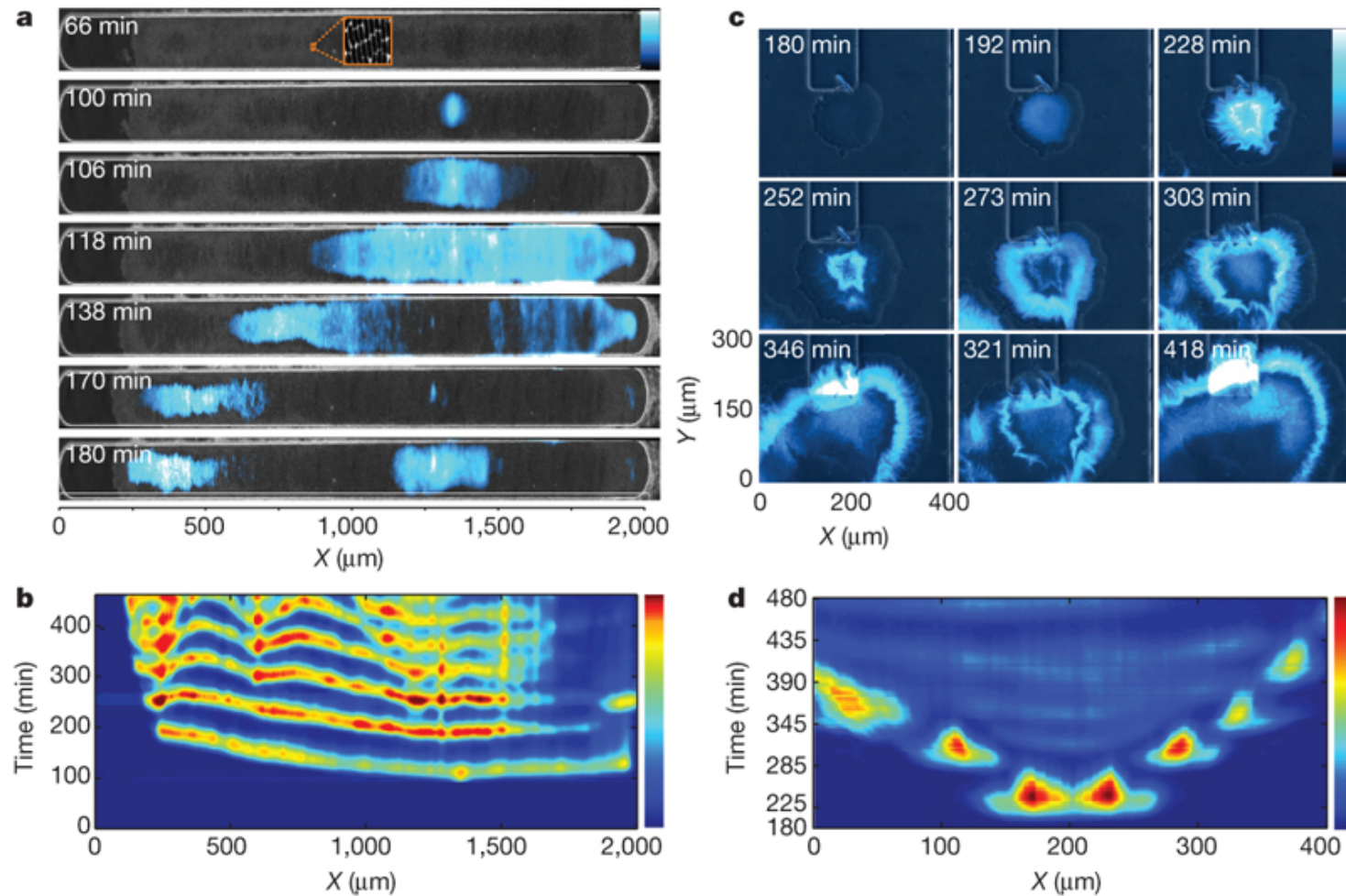


Tal Danino, Octavio Mondrago'n-Palomino, Lev Tsimring & Jeff Hasty, A synchronized quorum of genetic clocks, Nature, Vol 463| 21 (2010)

Dynamics under different microfluidic conditions



Spatiotemporal dynamics



Spatiotemporal models

